Mutual Exclusion Tokenless and Token Based Algorithms

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Outline

- Tokenless Algorithms
 - Ricart-Agarwala Algorithm
 - Maekawa's Algorithm
- Token Based Algorithms
 - Suzuki-Kasami Algorithm
 - Raymond's Tree Algorithm

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Motivation

- Lamport's algorithm required 3(N-1) messages.
- Insight:

Question

Do we really have to send a timestamped reply message?

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- Solution
 - Lamport's algorithm sent an acknowledgement immediately.
 - Let us hold on to the acknowledgement and piggy back it with a release message.
 - We can reduce the number of messages per critical section to 2(N-1).

Algorithm

Requesting the Lock

- P_i sends a timestamped request message to all other nodes.
- When P_i receives a request, it sends a reply if:
 - P_j is neither holding the lock, not is it interested in acquiring it. OR
 - P_i 's request timestamp is smaller than P_j 's request timestamp, and P_j is not holding the lock. (means that P_i made an earlier request)

Acquiring and Releasing the Lock

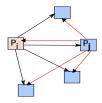
Acquiring the Lock

A process acquires the lock when it has received N-1 replies.

Releasing the Lock

A process replies to all pending requests after it releases the lock.

Proof



Proof

- Assume P_i and P_i both have a lock at the same time.
- Assume that P_i has a lower request timestamp.
- This means that P_i must have gotten P_j 's request after its request.
- According to the algorithm, P_i cannot send a reply to P_i.
- Hence, P_i does not have the lock.

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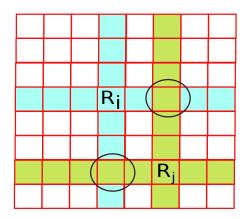
Can we do better?

- The main reason for a linear number of messages is:
 - We send a message to all the sites.
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- The main reason for a linear number of messages is:
 - We send a message to all the sites.
 - We also expect replies from all of them.
- Can we send a message to a subset of sites?
 - Let a set of processes associated with a process be called its request set (R_i).
 - For any two processes, P_i and P_j , we have: $R_i \cap R_j \neq 0$.
 - The minimum value of $|R_i|$ is \sqrt{N} .
 - It is possible to construct this using results from field theory.

Simpler construction $R_i = 2\sqrt{N}$



Acquiring a Lock

- P_i sends a timestamped request message to every node in R_i including itself.
- Upon receiving a request message a node $P_j \in R_i$ marks itself as locked, if it is not already locked. It returns a locked reply to P_i .

Acquiring a Lock

- P_i sends a timestamped request message to every node in R_i including itself.
- Upon receiving a request message a node $P_j \in R_i$ marks itself as locked, if it is not already locked. It returns a locked reply to P_i .
- If P_i is already locked by a request from P_k.
 - \bigcirc P_i places the request in a wait queue.
 - 2 If the locking request or any other request in the queue precedes the current request, then send a failed message.
 - 3 Otherwise, send an inquire message to P_k .

Acquiring a Lock - II

- When P_k receives an inquire message:
 - If P_k has received a failed message, and knows that it cannot succeed, it sends a relinguish message.
 - Otherwise, it defers the reply.

Acquiring a Lock - II

- When P_k receives an inquire message:
 - If P_k has received a failed message, and knows that it cannot succeed, it sends a relinquish message.
 - Otherwise, it defers the reply.
- When P_i receives the relinquish message:
 - 1 It locks itself for the earliest message from P'_i in its wait queue (might be P_i).
 - 2 It sends a locked message to P'_i .
 - 3 It adds the request from P_k to its wait queue.

Acquiring a Lock - II

- When P_k receives an inquire message:
 - If P_k has received a failed message, and knows that it cannot succeed, it sends a relinquish message.
 - Otherwise, it defers the reply.
- When P_i receives the relinquish message:
 - 1 It locks itself for the earliest message from P'_i in its wait queue (might be P_i).
 - 2 It sends a locked message to P'_i .
 - 3 It adds the request from P_k to its wait queue.
- A process acquires the lock when it has received locked messages from its entire request set.

Releasing the Lock

- A process sends released messages to all the processes in its request set.
- A process in the request set, locks itself for the earliest request in the wait queue. It sends it a locked message.
- If there is no such request, then it marks its status as unlocked.

Proof

Mutual Exclusion

Assume two processes P_i and P_i have the lock simultaneously.

- There must be a node P_k that must have given locked messages to both the processes.
- This is not possible.

Deadlock

Not possible because because we order the requests by their timestamp.

Starvation

Ultimately, a request will become the earliest message in the system.



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Main Idea

- A site can access the lock(critical section) if it has a token.
- Every process maintains a sequence number (request id)
 - A request is of the form (i, m). This means that P_i wants its mth access to the lock.
 - P_i keeps an array seq_i[1...N].
 - seq_i[j] is the largest sequence number received from j.
 - When P_i receives (j, m), it sets

$$seq_i[j] = max(seq_i[j], m)$$

- Token
 - A queue(Q) of requesting sites.
 - 2 An array of sequence numbers C.
 - C[i] is the sequence number of the latest request that P_i executed.



Requesting the Lock

Requesting the Lock

- P_i : $seq_i[i] + +$, $val \leftarrow seq_i[i]$
- Sends (i, val) to all sites
- When P_i receives (i, val)
 - $seq_i[i] \leftarrow max(seq_i[i], val)$
 - If the token is idle and with P_j then it sends it to P_i if $seq_j[i] \leftarrow C[i] + 1$.
- P_i enters the critical section when it has the token.

Releasing the Lock

Releasing the Lock

 P_i releases the lock as follows:

- $C[i] \leftarrow seq_i[i]$
- $\forall j$, adds P_i to Q if $seq_i[j] = C[j] + 1$.
- Dequeues P_k from Q, and sends the token to P_k

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Message Overhead: 0 or N

Proof

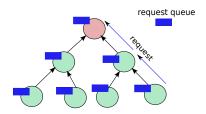
A requesting process gets the lock in finite time.

- The request will reach all the processes in finite time.
- By induction, one of these processes will have the token in finite time.
- Thus the current request will get added to Q.
- There can at most be N-1 messages before it.

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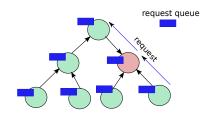
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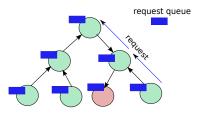
Main Idea



- Nodes are arranged as a tree. Every node has a parent pointer.
- Each node has a FIFO queue of requests.
- There is one token with the root and the owner of the token can enter the critical section.
- Message Complexity: approximately O(log(N)) for trees with high fan-out

Dynamic Nature of the Tree





- As the token moves across nodes, the parent pointers change.
- They always point towards the holder of the token.
- It is thus possible to reach the token by following parent pointers.

Requesting for the Token

Requesting a Token

- The node adds "self" in its request queue.
- Forwards the request to the parent.
- The parents adds the request to its request queue.
- If the parent does not hold the token and it has not sent any requests to get the token, it sends a request to its parent for the request.
- This process continues till we reach the root (holder of the token).

Releasing a Token

Releasing a Token

- Ultimately a request will reach the token holder.
- The token holder will wait till it is done with the critical section.
- It will forward the token to the node at the head of its request queue.
 - It removes the entry.
 - It updates its parent pointer.
- Any subsequent node will do the following:
 - Dequeue the head of the queue.
 - If "self" was at the head of its request queue, then it will enter the critical section.
 - Otherwise, it forwards the token to the dequeued entry.
- After forwarding the entry, a process needs to make a fresh request for the token, if it has outstanding entries in its request queue.



Correctness

Mutual Exclusion

No two nodes can have a token at the same time, and thus cannot be in the CS at one time.

Deadlock

- Circular wait cannot occur because all the nodes wait on the node that holds the token.
- Messages cannot get lost because all the time our parent pointers ensure that we have a rooted tree.

Starvation

- Ultimately a starved process's request will come to the front of all the request queues.
- At this point it will have the highest priority, and the token will have to flow back to the starved process.



A \sqrt{N} Algorithm for Mutual Exclusion in Decentralized Systems by Mamoru Maekawa, ACM Transactions on Computer Systems, 1985