

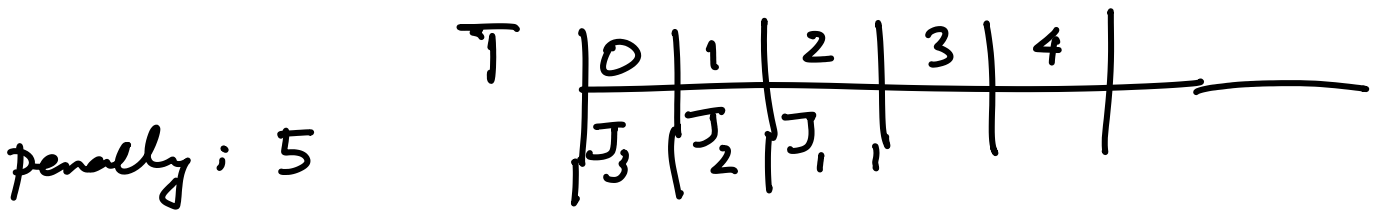
Scheduling problem

Given a set of n jobs J_1, J_2, \dots, J_n with processing requirements 1 unit and (integral) deadlines, we want to schedule them in a way so that they get completed before deadlines. If not then job J_i incurs a penalty p_i . Goal: Minimize penalty.

Eg.

	J_1	J_2	J_3
deadlines	1	2	1
penalty	5	2	8

(only one job can be running at a time)



Strategy: Earliest deadline first
break ties on the basis of penalty

Suppose we have a schedule
 $t_1 \quad t_2 \quad \dots \quad t_i \quad \dots \quad t_k$
 $j_1 \quad j_2 \quad j_3 \quad \dots \quad j_i \quad \dots \quad j_k \quad \dots$

$$d_i > d_k$$


If $d_i < t_k$ then we may
incur penalty

Suppose the given schedule is "feasible"
(no job incurs penalty) then

$$d_k > t_k \quad d_i > d_k \Rightarrow d_i > t_k$$

Objective: Minimize the penalty of
the jobs that missed the
deadline

\Leftrightarrow maximise the penalty of the
"feasible" schedule

To apply "generic greedy" we must
define the subset system framework

$$S = \{J_1, J_2, \dots, J_n\}$$

I : subsets of S that are "feasible", i.e. they can be scheduled without missing any deadline.

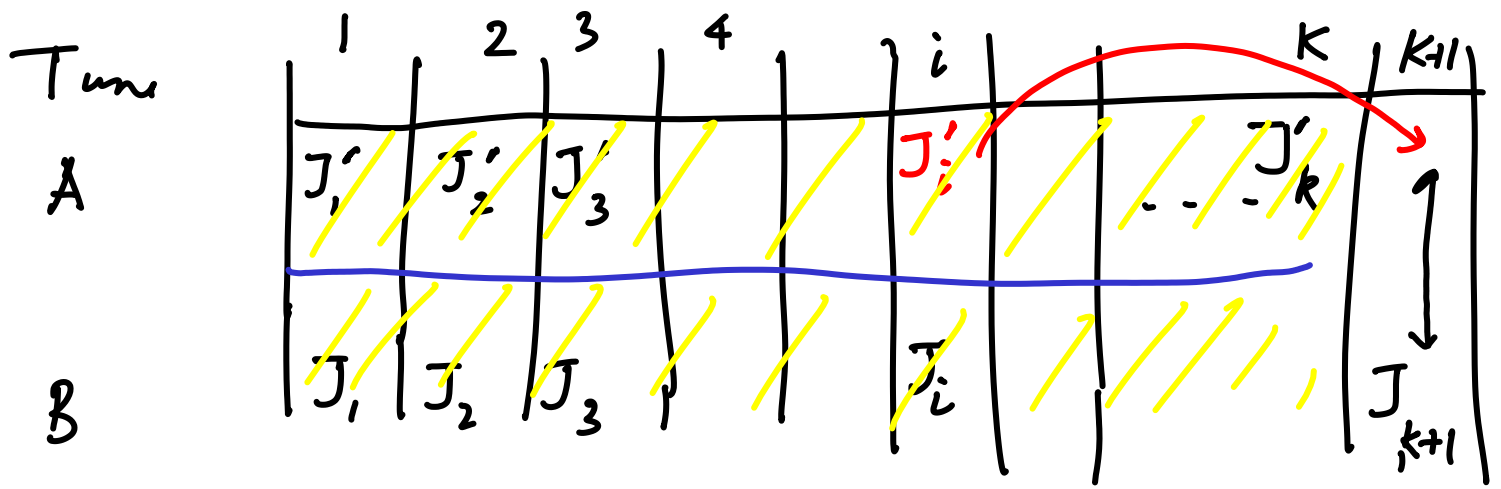
Moreover, any subset of a feasible set of jobs is also feasible.

We would like to see if we can satisfy properties (2) or (3) of the matroid theorem.

exchange property.

Given feasible sets A and B

$|B| > |A|$ can we add a job $j \in B - A$ to A and still keep $A \cup \{j\}$ feasible?



Case 1 : $J_{k+1} \notin A$ add J_{k+1} to A

Case 2 $J_{k+1} \in A \Rightarrow J_{k+1} = J'_i$

Repeat the same argument with one job less in A and B.

either we terminate with case 1 or we are in a situation where $A = \emptyset$ and B has 1 job

h.w : Find a feasible schedule (the above argument gives a feasible set)

"Greedy works"

How about minimizing in the matroid framework?

Since \emptyset is independent by defn
 \emptyset is the min wt = 0

To deal with min. spanning trees,
the underlying graph must be
connected.

Then max spanning forest is
a max spanning Tree.

Redefine the wt function

$$\text{as } w(e) = w_{\max} - w(e)$$

w_{\max} is the maximum wt of any edge.