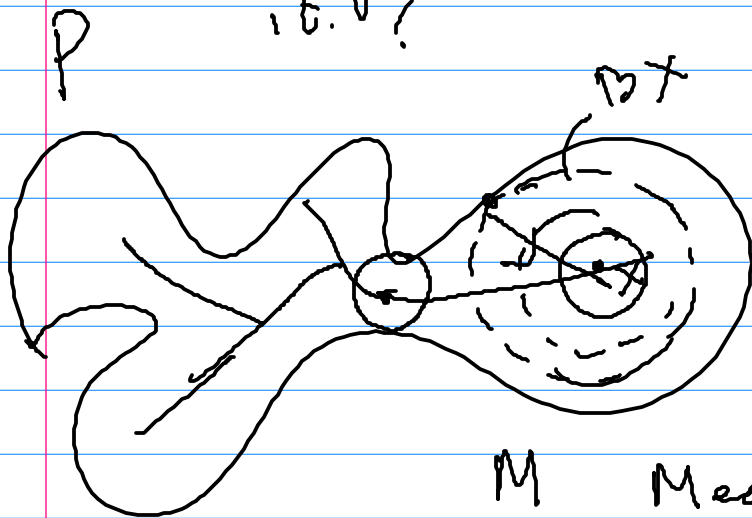


# Lecture 39: Shape Representation

## Sampling

How densely one should sample a geometric shape to reconstruct it.?



• Medial axis

• Local feature size.

$B_x$ : smallest ball at  $x$  that touches  $\partial P$ .

$M$  Medial axis of  $P$

$$M = \{x \mid |B_x \cap \partial P| > 1\}$$

If  $\partial P$  is connected, Medial axis of  $P$  is a tree.

Retraction  $Q: \mathbb{R}^2 \rightarrow M$

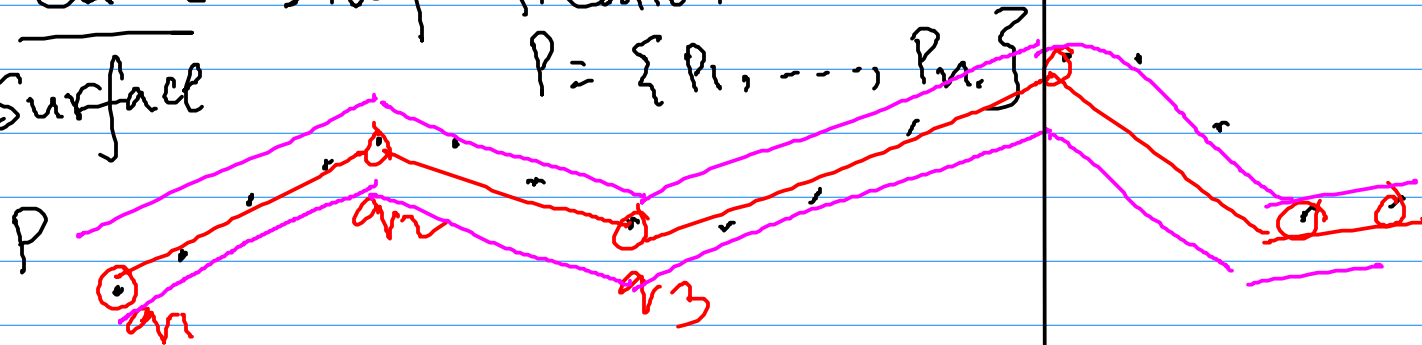
$$Q(p) = x \text{ if } p \in B_x \cap \partial P$$

$$LFS(p) = \|p - Q(p)\|$$

around  $p$

Sampling density  $\propto \frac{1}{LPCS(p)}$

Curve Simplification  
Surface



$\epsilon$ : tolerance error

$Q \subseteq P$      $Q = \{q_1, \dots, q_k\}$

each  $p_i$  has within distance  $\epsilon$  from  
in chain  $q_1 q_2 \dots q_k$

$k$  should be small.

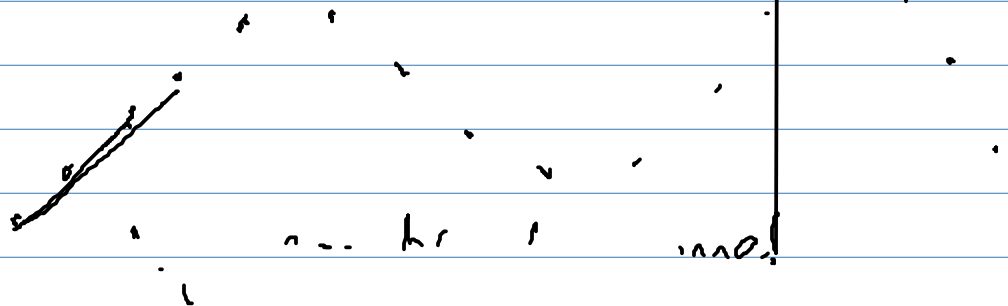
- Refinement
- Decimation

n

# Douglas-Peucker algorithm

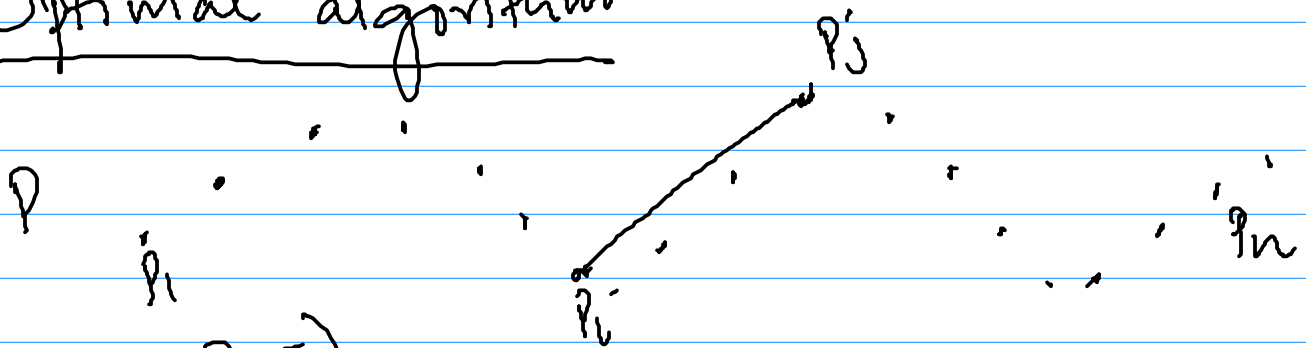


Decimation Method



Edge contraction method.

Optimal algorithm



$$G = (P, E)$$

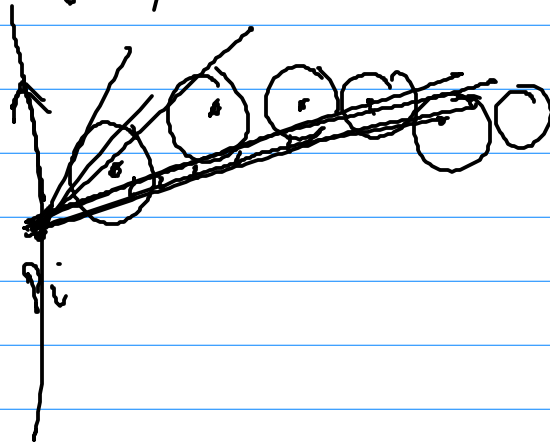
$$(P_i, P_j) \in E \text{ if}$$

$$d(P_k, \overline{P_i P_j}) \leq \epsilon \quad \forall i \leq k \leq j$$

Find the shortest path from  $P_1$  to  $P_n$   
in  $G$ .

$O(n^3)$  : straightforward.

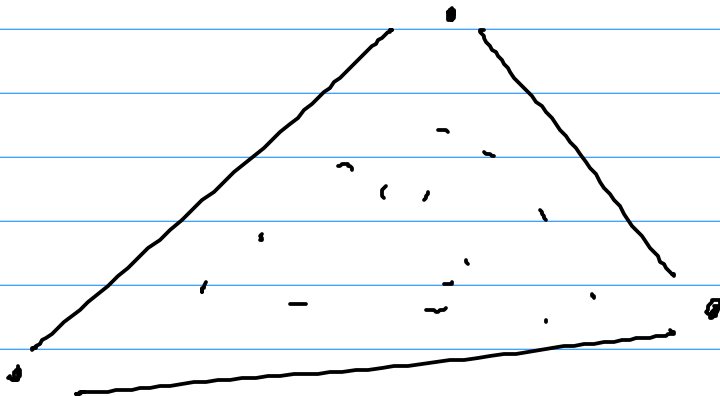
$O(n^2 \log n)$



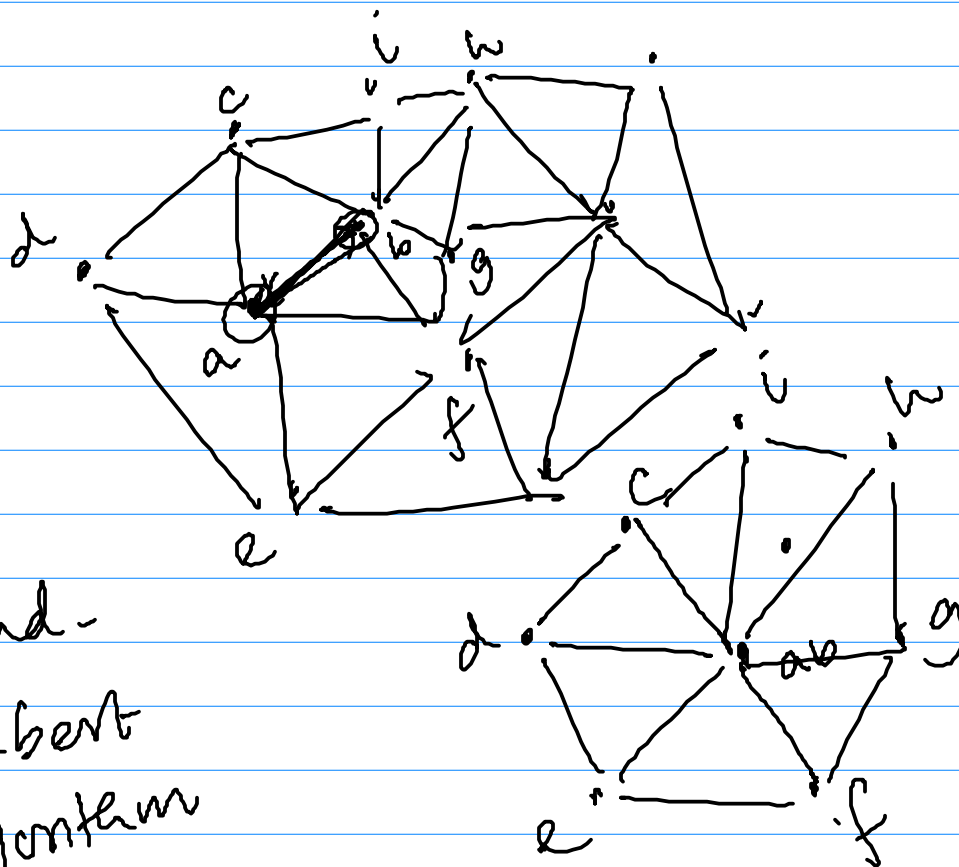
$n^{4/3}$

Chebyshev  
metric

## Surface Simplification



# Decimation method.



Garland-  
Heckbert  
algorithm