Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)

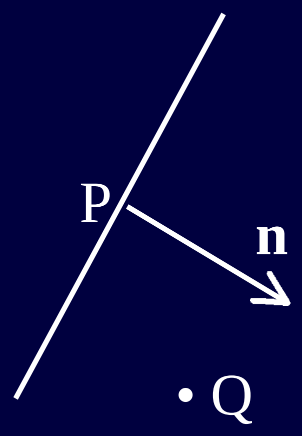
- Any convex region as window

Parametric line (input line AB):

$$L(t) = A + (B - A)t; t \in (0,1)$$

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)



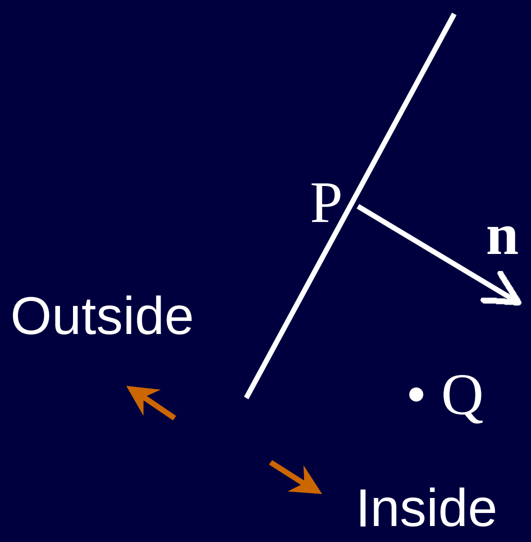
Implicit line (window edge):

$$\boldsymbol{l(Q) = (Q - P).n}$$

Tells us on which side of the line the point Q is.

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)



Evaluate

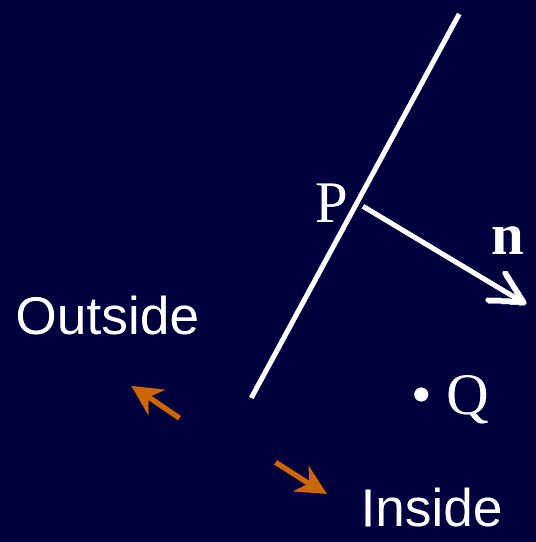
$$I(Q) = (Q - P).n$$

If > 0 inside halfspace of line (plane)
If < 0 outside halfspace of line (plane)
If = 0 on the line

Should give indications for trivial accept and reject cases.

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)



Window edge $I(Q) = (Q - P).n$

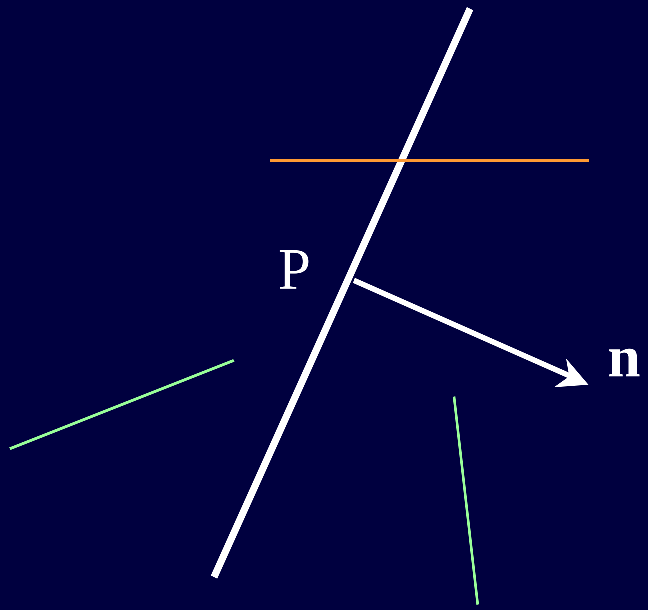
Line segment $L(t) = A + t(B - A)$

Trivial Reject $I(A) < 0 \text{ AND } I(B) < 0$

Trivial Accept $I(A) > 0 \text{ AND } I(B) > 0$

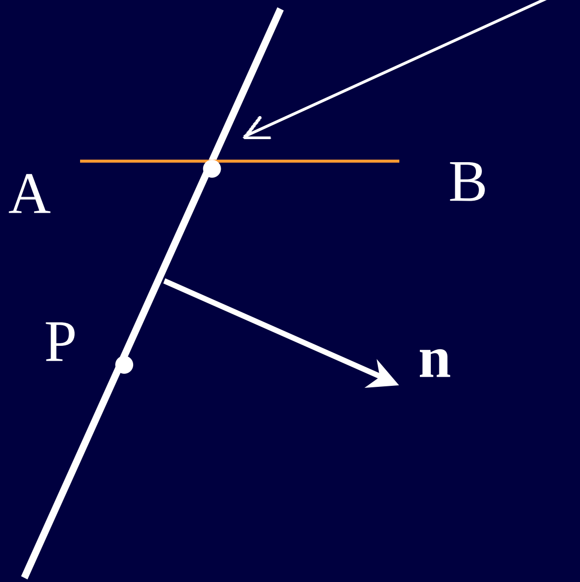
Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)



Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)



$$L(t) = A + (B - A)t$$

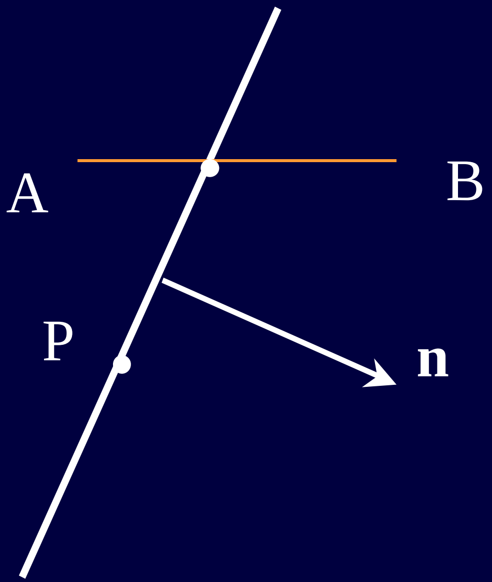
$$l(Q) = (Q - P).n$$

$$l(L(t)) = 0; \text{solve for t}$$

$$(L(t) - P).n = 0$$
$$(A + t(B - A) - P).n = 0$$
$$(A - P).n + t(B - A).n = 0$$

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)

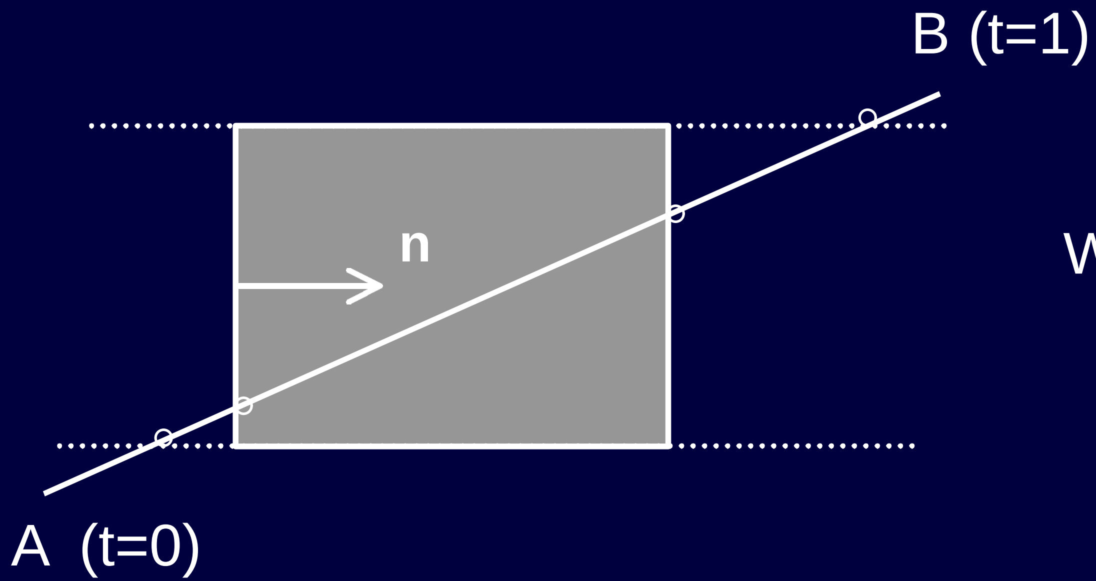


$$t = \frac{(A - P).n}{(A - B).n}$$

$$t = \frac{(A - P).n}{(A - P).n - (B - P).n}$$

Clipping

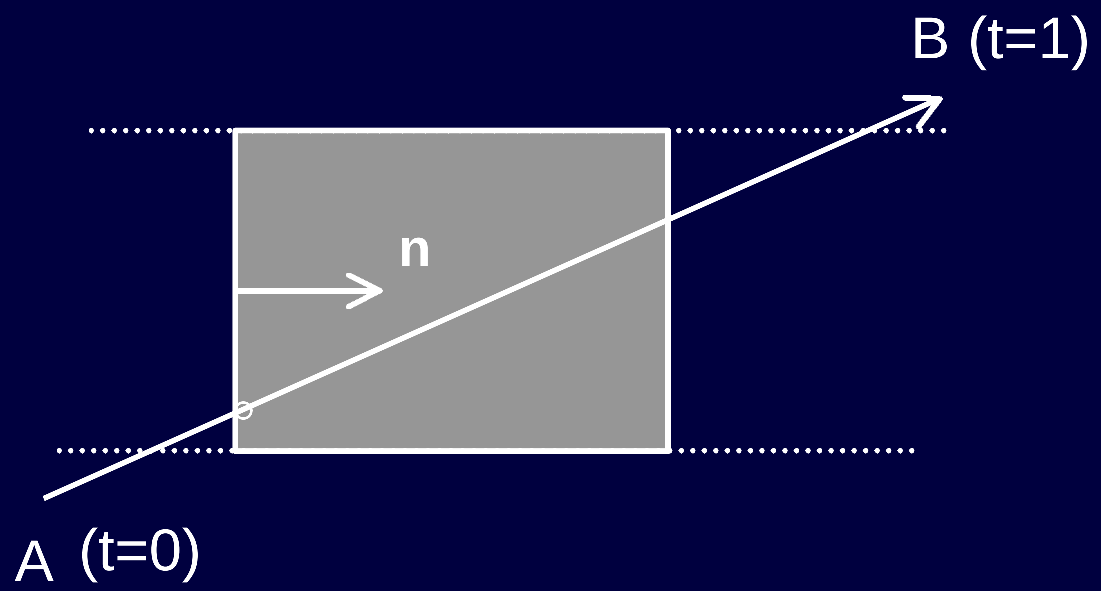
Cyrus Beck Line Clipping
(Liang and Barsky)



Which ‘t’ to select ?

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)



$$\boldsymbol{t} = \frac{(\boldsymbol{A}-\boldsymbol{P}).\boldsymbol{n}}{-(\boldsymbol{B}-\boldsymbol{A}).\boldsymbol{n}}$$

$$\boldsymbol{D} = (\boldsymbol{B}-\boldsymbol{A}).\boldsymbol{n}$$

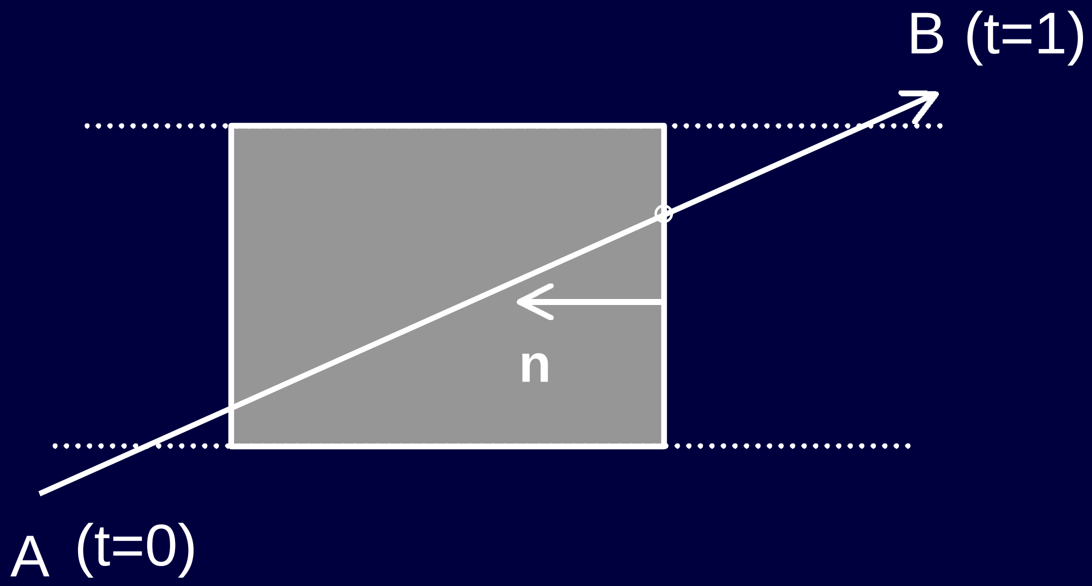
D > 0 label t as t_E

Entering

Clipping

Cyrus Beck Line Clipping

(Liang and Barsky)



$$t = \frac{(A - P).n}{-(B - A).n}$$

$$D = (B - A).n$$

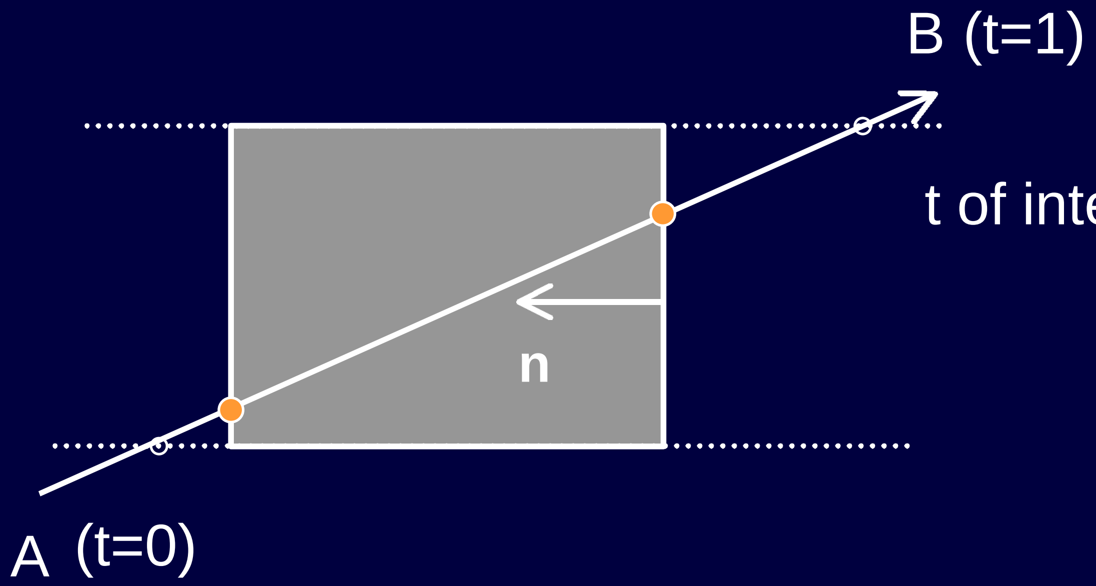
D < 0 label t as t_L

Leaving

Clipping

Cyrus Beck Line Clipping

(Liang and Barsky)



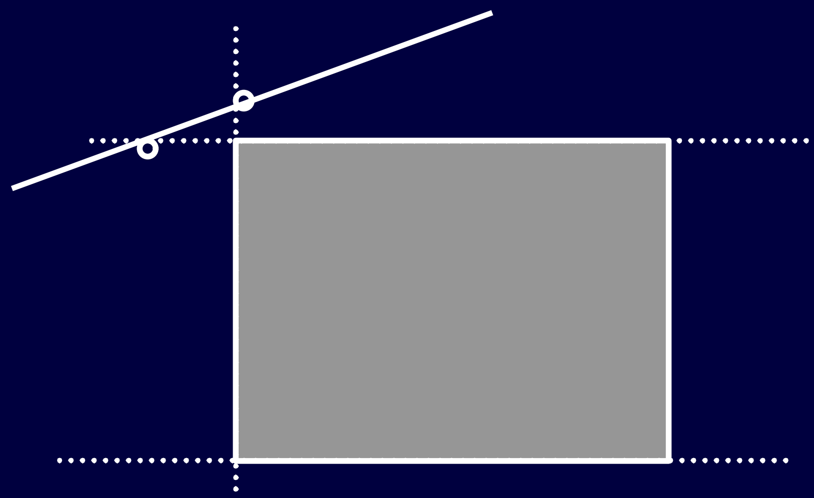
t of interest:

largest t_E t_E^{max}

smallest t_L t_L^{min}

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)



If $t_E^{max} > t_L^{min}$

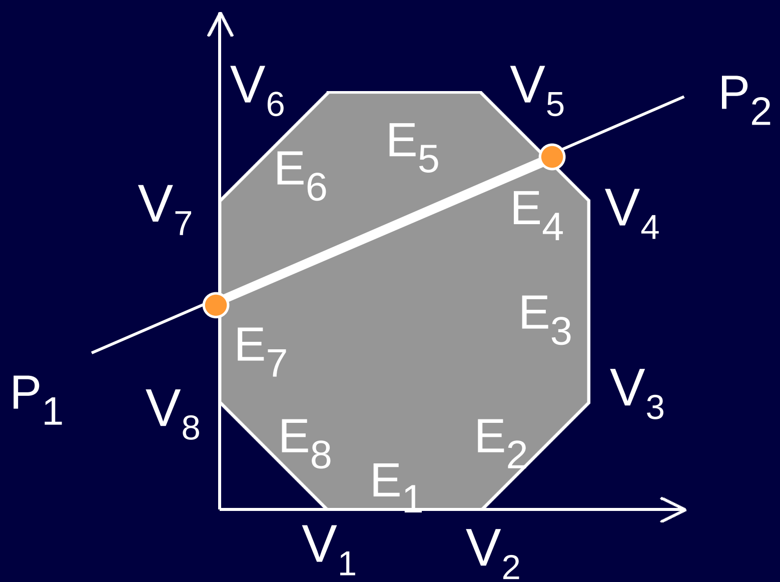
Reject

Clipping

Cyrus Beck Line Clipping

(Liang and Barsky)

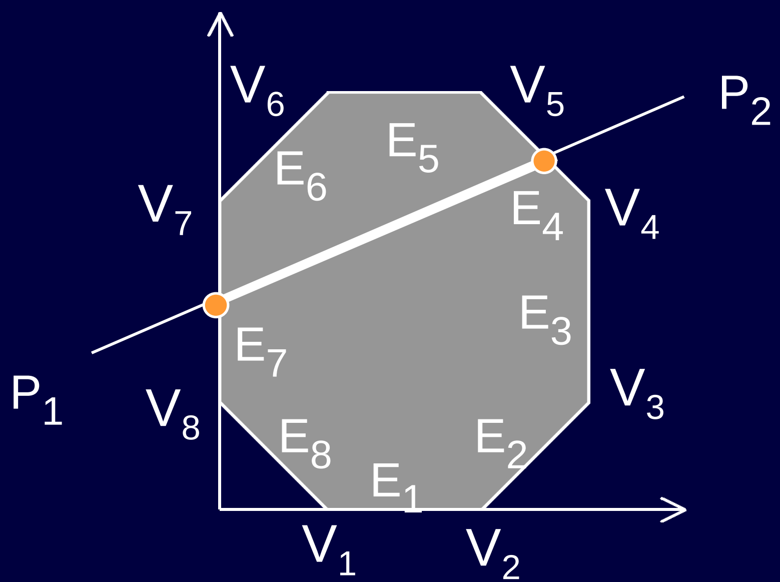
Arbitrary Convex Window



Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)

Arbitrary Convex Window



$E_1 x E_2$: positive

$E_2 x E_3$: positive

.

.

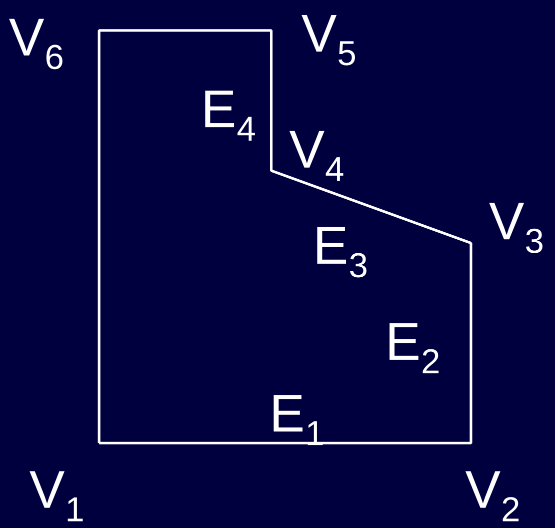
.

Polygon is convex if for all adjacent edges the sign of cross product is same.

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)

Arbitrary Window



$E_1 x E_2$: positive
$E_2 x E_3$: positive
$E_3 x E_4$: negative

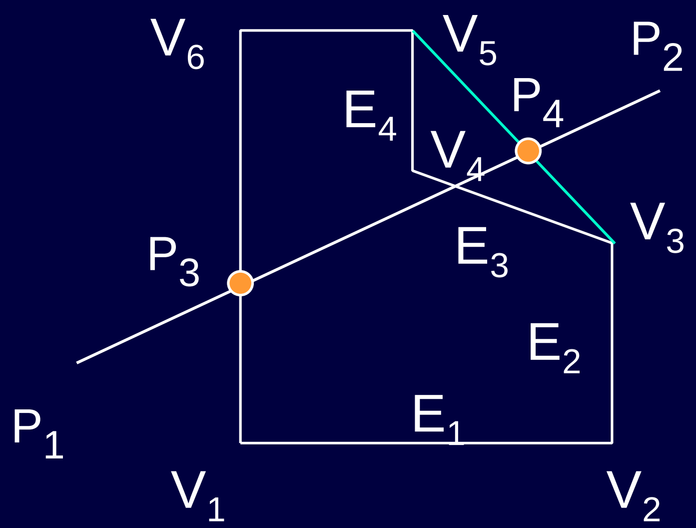
.
.
.

Polygon is non-convex

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)

Arbitrary Window



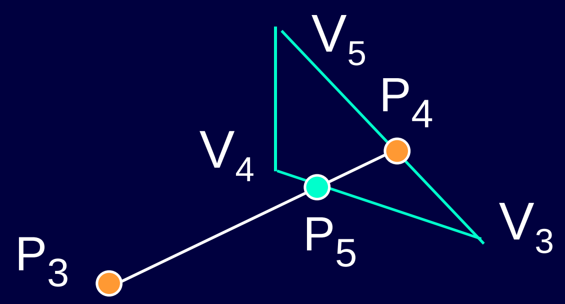
Make the polygon convex by adding the edge V_3V_5

Clip against the convex polygon => P_3P_4

Clipping

Cyrus Beck Line Clipping
(Liang and Barsky)

Arbitrary Window



Clip against the triangle
=> P_5P_4

Subtract P_5P_4 from P_3P_4
=> P_3P_5