In these two assignments, we will design a data structure that will help us solve a simplified version of the mobile phone tracking problem, i.e., the fundamental problem of cellular networks: When a phone is called, find where it is located so that a connection may be established.

Mobile phone tracking system description

As we know each mobile phone that is switched on is connected to the base station which is nearest. These base stations are popularly called cell phone towers. Although sometimes we may be within range of more than one base station, each phone is registered to exactly one base station at any point of time. When the phone moves from the area of one base station to another, it will be de-registered at its current base station and re-registered at new base station.

Making a phone call. When a phone call is made from phone $p_1$ registered with base station $b_1$ to a phone $p_2$, the first thing that the base station $b_1$ has to do is to find the base station with which $p_2$ is registered. For this purpose there is an elaborate technology framework that has been developed over time. You can read more about it on the Web. But, for now, we will assume that $b_1$ sends a query to a central server $C$ which maintains a data structure that can answer the query and return the name of the base station, let’s call it $b_2$, with which $p_2$ is registered. $C$ will also send some routing information to $b_1$ so that $b_1$ can initiate a call with $b_2$ and, through the base
stations $p_1$ and $p_2$ can talk. It is the data structure at $C$ that we will be implementing in this assignment.

**A hierarchical call routing structure.** We will assume that geography is partitioned in a hierarchical way. At the lowest level is the individual base station which defines an area around it such that all phones in that area are registered with it, e.g., all phones that are currently located in Bharti building, School of IT and IIT Hospital are registered with the base station in Jia Sarai. This base station also serves phone in Jia Sarai and maybe some phones on Outer Ring Road in front of Jia Sarai. Further we assume that base stations are grouped into geographical locations served by an level 1 area exchange. So, for example, the Jia Sarai base station may be served by the Hauz Khas level 1 area exchange. Each level $i$ area exchange is served by a level $i+1$ area exchange which serves a number of level $i$ area exchanges, e.g., the Hauz Khas level 1 area exchange and the Malviya level 1 area exchange may be both served by a South-Central Delhi level 2 area exchange. A base station can be considered to be a level 0 area exchange in this hierarchical structure. Given a level $i$ exchange $f$, we say that the level $i + 1$ exchange that serves it is the parent of $f$, and denote this parent$(f)$.

We will call this hierarchical call routing structure the *routing map* of the mobile phone network.

**Maintaining the location of mobile phones.** Every level $i$ area exchange, $e$, maintains a set of mobile phones, $S_e$, as follows. The set $S_e$ is called the *resident set* of $e$. The level 0 area exchanges (base stations) maintain the set of mobile phones registered directly with them. A level $i + 1$ area exchange $e$, maintains the set $S_e$ defined as follows

$$s_e = \bigcup_{\text{parent}(f) = e} S_f,$$

i.e., the union of the sets of mobile phones maintained by all the level $i$ area exchanges it serves.

Clearly, the root of the routing map maintains the set of all currently registered mobile phones.

**Tracking a mobile phone.** The routing map along with the resident sets of each area exchange makes up the mobile phone tracking data structure we
will be using. This data structure will be stored at the central server \( C \). The process of tracking goes as follows.

- When a base station \( b \) receives a call for a mobile phone with number \( m \) it sends this query to \( C \).

- If the root of the routing map is \( r \), we first check if \( m \in S_r \). If not then we tell \( b \) that the number \( m \) is “not reachable.”

- If \( m \in S_r \) we find that \( e \) such that parent(\( e \)) = \( r \) and \( m \in S_e \), i.e. we find the child of \( r \) which contains \( m \) in its resident set.

- Continue like this till we reach all the way down to a leaf of the routing map. This leaf is a base station \( b' \). The central server sends \( b' \) to \( b \) along with the path in the routing map from \( b \) to \( b' \).

**The programming assignments**

We now describe the implementation details of the system defined above. This is split into two programming assignments, #2 and #3. Please note the different deadlines for these assignments.

**Assignment 2**

**Deadline: 11:55 PM, 21 September 2015**

- Write a java class called \texttt{Myset} that implements sets, with the following methods:
  - public Boolean IsEmpty(): returns true if the set is empty.
  - public Boolean IsMember(Object o): Returns true if \( o \) is in the set, false otherwise.
  - public void Insert(Object o): Inserts \( o \) into the set.
  - public void Delete(Object o): Deletes \( o \) from the set, throws exception if \( o \) is not in the set.
  - public Myset Union(Myset a): Returns a set which is the union of the current set with the set \( a \).
public Myset Intersection(Myset a): Returns a set which is
the intersection of the current set with the set a.
You may use a linked list of objects to implement the Myset class.
Note that Object is the fundamental class in Java. You can cast
it to any class that you want (Integer, Float, Double, etc).

Demo instructions: Write your code for set in a file named
Myset.java. Ensure that the name of the functions and the type of
the function arguments/return type should be same as mentioned
here. Implement the linked list yourself. You may copy the code
for linked lists out of the book or any other source.

Optional challenge problem: Bloom filters are an efficient data
structure for implementing the class Myset. Look up Bloom filters
on the web and write an alternate implementation of the Myset
class which uses Bloom filters instead of linked lists. Keep in
mind that the results of the IsMember() method in a Bloom filter
implementation of a set have an error in them. How does this
affect the working of the overall system? How can you account for
this?

• Write a java class called MobilePhone, with the following methods:

  - MobilePhone(Int number): constructor to create a mobile
    phone. Unique identifier for a mobile phone is an integer.
  - public Int number(): returns the id of the mobile phone.
  - public Boolean status(): returns the status of the phone, i.e.
    switched on or switched off.
  - public void switchOn(): Changes the status to switched on.
  - public void switchOff(): Changes the status to switched off.
  - public Exchange location(): returns the base station with which
    the phone is registered if the phone is switched on and an excep-
    tion if the phone is off. The class Exchange will be described
    next.

• Create a class MobilePhoneSet which stores MobilePhone objects in a
  Myset.
• Create a class **ExchangeList** which implements a linked list of exchanges.

• Write a java class **Exchange** that will form the nodes of the routing map structure. The class should have the following methods.

  - **Exchange(Int number):** constructor to create an exchange. Unique identifier for an exchange is an integer.
  - All usual **Node** methods for a general tree like **public Exchange parent(),** public **Exchange numChildren()** (for number of children), public **Exchange child(int i)** (returns the \(i\)th child), **public Boolean isRoot(),** public **RoutingMapTree subtree(int i)** (returns the \(i\)th subtree) and any other tree methods you need. The class definition **RoutingMapTree** will be defined later.
  - **public MobilePhoneSet residentSet():** This returns the resident set of mobile phones of the exchange.

• Write a java class **RoutingMapTree** which is a tree class whose nodes are from the **Exchange** class. The class should contain the following:

  - **RoutingMapTree():** constructor method. This should create a RoutingMapTree with one Exchange node, **the root node which has an identifier of 0.** Create other constructors that you deem necessary.
  - All general tree methods like **public Boolean containsNode(Exchange a)** but with **Exchange** as the node class.
  - **public void switchOn(MobilePhone a, Exchange b):** This method only works on mobile phones that are currently switched off. It switches the phone \(a\) on and registers it with base station \(b\). The entire routing map tree will be updated accordingly.
  - **public void switchOff(MobilePhone a):** This method only works on mobile phones that are currently switched on. It switches the phone \(a\) off. The entire routing map tree has to be updated accordingly.
  - **public void performAction(String actionMessage):** This the main stub method that you have to implement. It takes an action as a string. The list of actions, and their format will be described next.
**Demo instructions:** In this assignment, you are given just three files: assn2checker.java, RoutingMapTree.java and actions.txt. assn2checker.java file is our program which reads the input actions from the actions.txt file, and feeds them to RoutingMapTree.java. You have to create the file for other classes. Each class file should contain the methods that we have explicitly mentioned in the problem statement. You can implement other functions too if you want.

In this assignment, we are not going to use an automated check script. The primary task of your assignment is to give the correct answer to the query messages (described later). We will verify the output of the program during the demo. Here is a list of action messages that you need to handle:

- **addExchange a b** This should create a new Exchange b, and add it to the child list of Exchange a. If node a has n children, b should be its \((n + 1)^{th}\) child. If there is no Exchange with identifier a, then throw an Exception.

- **switchOnMobile a b** This should switch ON the mobile phone a at Exchange b. If the mobile did not exist earlier, create a new mobile phone with identifier a. If there is no Exchange with an identifier b, throw an exception.

- **switchOffMobile a** This should switch OFF the mobile phone a. If there is no mobile phone with identifier a, then throw an Exception.

- **queryNthChild a b** This should print the identifier of the Exchange which is the \((b)\)th child of Exchange a.

- **queryMobilePhoneSet a** This should print the identifier of all the mobile phones which are part of the resident set of the Exchange with identifier a.

**Points to note:**

- Your program’s response should be printed inside the `performAction` method of the `RoutingMapTree` class. Use the `System.out.println()` method to print the output. For the given actions.txt file, we have provided a answers.txt file showing the expected format of the program response.
• If the code discovers that there is an inconsistent action being performed, instead of just exiting, you should print an error message, and continue with program execution. Example of an inconsistent action can be switching off a mobile that does not exist. It will be better if you handle such inconsistent states by raising suitable Exception in the implementing class (Set/Exchange), and handling it in the RoutingMapTree class. Read relevant text on the web to know more about raising and handling Exceptions.

• We will be using a different actions.txt file in the demo. So make sure that your program considers all conditions before you submit it on Moodle. If you have formatting issues in using this file on Windows/MacOS platform, create a suitable version of the same file for your platform. By formatting, we mean the new-line/space/tab-space.

Assignment 3
Deadline: 11:55 PM, 26 September 2015

In this assignment we move on to implementing the details of the tracking system. Implement the following additional methods in the RoutingMapTree class.

• public Exchange findPhone(MobilePhone m): Given a mobile phone m it returns the level 0 area exchange with which it is registered or throws an exception if the phone is not found or switched off.

• public Exchange lowestRouter(Exchange a, Exchange b): Given two level 0 area exchanges a and b this method returns the level i exchange with the smallest possible value of i which contains both a and b in its subtree. If a = b then the answer is a itself.

• public ExchangeList routeCall(MobilePhone a, MobilePhone b): This method helps initiate a call from phone a to phone b. It returns a list of exchanges. This list starts from the base station where a is registered and ends at the base station where b is registered and represents the shortest route in the routing map tree between the two base stations. It goes up from the initiating base station all the way to the lowestRouter connecting the initiating base station to the final base station and then down again. The method throws exceptions as appropriate.
• **public void movePhone(MobilePhone a, Exchange b):** This method modifies the routing map by changing the location of mobile phone a from its current location to the base station b. Note that b must be a base station and that this operation is only valid for mobile phones that are currently switched on.

**Demo instructions:** The evaluation framework for assignment 3 is same as assignment 2. We have added extra action messages to test the mobile tracking system. Here is a list of the extra action messages that your RoutingMapTree should support.

• **queryFindPhone a** This should print the identifier of the exchange returned by the findPhone(MobilePhone m) method. Here, m represents the mobile phone whose identifier is a.

• **queryLowestRouter a b** This should print the identifier of the exchange returned by the lowestRouter(Exchange e1, Exchange e2) method. Here, e1 and e2 represent exchanges with identifier a and b respectively.

• **queryFindCallPath a b** This should print the list returned by the routeCall(MobilePhone m1, MobilePhone m2) method. Here, m1 and m2 represent mobile phones with identifier a and b respectively. Successive entries in the list should be separated by a comma.

• **movePhone a b** This action should set the level 0 area exchange of the mobile phone with identifier a to exchange with identifier b. Throw exception if mobile a is not available, or exchange b does not exist.

Consider all possible scenarios for each action message. When an inconsistent action is triggered, your code should display suitable error message, and continue with the next action message.

**Note:** Your program’s response should be printed inside the `performAction` method of the `RoutingMapTree` class. Use the `System.out.println()` method to print the output. For the given actions.txt file, we have provided a answers.txt file showing the expected format of the program response.

**Optional challenge problem:** If you want you can make this whole thing much closer to reality by writing a multithreaded implementation of the entire system. Do the following:
• Learn how to write multithreaded programs in Java. There are many useful texts for this on the Web.

• Write an implementation which creates one thread for each mobile phone and one thread for the central server.

• The central server thread maintains the routing map tree.

• Each individual mobile phone thread is either in waiting mode, or it initiates a call, changes status from on to off or vice versa, or moves from one base station to another. Whenever it does this it has to communicate with the central server thread.

• Implement the mobile phone thread so that it generates a random operation request after a random amount of time.

• In order to make this more realistic you may have to introduce a new kind of status field which is on when the phone is on an active call and off otherwise. When a call is initiated by a phone, your multithreaded implementation should send a message to the destination phone which can accept or reject the request based on its on/off/busy status. Once the call is accepted both the phones become busy. In your implementation the calls should go on for a random amount of time.

• Create a dashboard that allows you to view the status of the system.

If you want to increase the challenge level further you can write individual threads for each area exchange. The root area exchange then becomes the one that each base station communicates with in case of a call request or a location/status update. How do you keep all the information of the routing map consistent? How does the routing map structure change? Many interesting questions will need to be answered.