

CS105L: Discrete Structures
I semester, 2006-07

Tutorial Sheet 7: Recurrences

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1. Let a_r denote the number of subsets of $\{1, 2, \dots, r-1, r\}$ which do not contain two consecutive numbers. Determine a_r .
2. There are two types of particles inside a nuclear reactor. In every second an α particle will split into three β particles and every β particle will split into an α particle and two β particles. If there is a single α particle at time $t = 0$ then how many particles are there in all at time $t = 100$?
3. Solve the following difference equations:
 - (a) $a_r^2 - 2a_{r-1}^2 = 1$, given that $a_0 = 2$.
 - (b) $a_r^2 - 2a_{r-1} = 0$, given that $a_0 = 4$.
 - (c) $a_r = \sqrt{a_{r-1} + \sqrt{a_{r-2} + \sqrt{a_{r-3} + \sqrt{\dots}}}}$, given that $a_0 = 4$.